

Mandatory vs. Voluntary a priori Investment in Information Acquisition in Procurement Auctions

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Outline

- ① Introduction
- ② Methods
- ③ Results
- ④ Conclusion

Background and motivation

- Procurement auctions are crucial for securing goods/services at competitive prices
- Key challenge: High uncertainty for bidders regarding future costs, particularly prominent in renewable energy auctions
- Common practice: certain prequalification prior to entering the auction (Kreiss et al. 2017)
⇒ a priori investment in information acquisition
- Impact of the mandatory setting:
 - Reduce uncertainties regarding future costs
 - Reduce participation and competition (Samuelson 1985)
 - Exclude potential interested bidders, leading to inefficiency
- Alternative: voluntary setting, e.g., German photovoltaic auctions (Bundestag 2017)
- **Research question:** Mandatory vs. voluntary a priori investment in information acquisition

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Related literature

● Auctions with participation costs

- Pure strategy (cutoff strategy): Samuelson (1985), McAfee and McMillan (1987), Tan and Yilankaya (2006), Celik and Yilankaya (2009), and Gillen et al. (2017)
- Mixed strategy (randomized participation): Levin and Smith (1994), Menezes and Monteiro (2000), and Jehiel and Lamy (2015)

● Information acquisition before or during auctions

- General: Stegeman (1996), Persico (2000), Bergemann and Välimäki (2002), and Schweizer and Szech (2017)
- Static vs. dynamic auction: Compte and Jehiel (2007), Gretschnko and Wambach (2014), and Gretschnko and Simon (2024)

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Model

- Single-unit second-price procurement auction
- $N \geq 2$ risk-neutral firms (potential bidders)
- Each firm has private costs x_i , which are a priori unknown to the firm
- x_i is the realization of the random variable $X_i, i \in \{1, \dots, N\}$, i.i.d. on $[\underline{x}, \bar{x}]$ with F and f
- The realization of X_i can only be known after an investment $c \geq 0$ in information acquisition
- The auctioneer has the maximum WTP $x_0, x_0 > \underline{x}$ and sets a reserve price $r \leq x_0$

Settings

Mandatory setting:

- The auctioneer requires a priori investment in information acquisition
- For participants: c is sunk costs and x_i is known $\Rightarrow \beta(x_i) = x_i$ if $x_i \leq r$

Voluntary setting

- An investment in information acquisition is voluntary, except for the winner
- For investors: c is sunk costs and x_i is known $\Rightarrow \beta(x_i) = x_i$ if $x_i \leq r$
- For non-investors: only the distribution of X_i is known $\Rightarrow \beta = \mathbb{E}[X_i] + c$ if $\mathbb{E}[X_i] + c \leq r$
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Possible symmetric equilibria

Our analysis identifies five types of symmetric equilibria depending on c and r

- E_0 : No participation
- E_1^f : Full participation, all firms participate and invest c
- E_1^r : Randomized participation, all firms participate and invest c with probability $q \in (0, 1)$
- E_2 : All firms participate without investment with probability $q' \in (0, 1]$
- E_{mix} : All firms participate and invest c with probability $q_1 \in (0, 1)$ and participate without investment with $q_2 \in (0, 1)$, $q_1 + q_2 \leq 1$.

Different equilibria depending on c and r

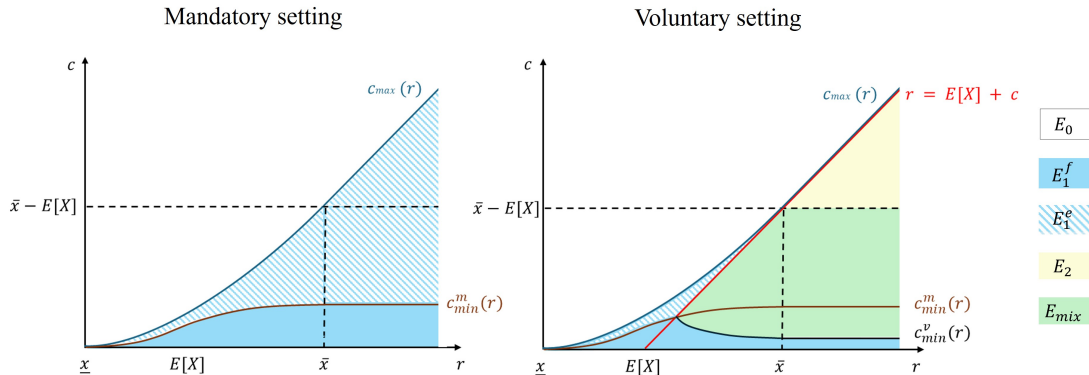


Figure: Different equilibria depending on c and r in mandatory and voluntary settings

Comparison between mandatory and voluntary settings

- **Expected participation:** voluntary setting $\succeq$ mandatory setting
- **Expected a priori investment:** voluntary setting $\leq$ mandatory setting
- **Optimal reserve price:** different locally optimal reserve prices

- E_1^f : $r^* = x_0 - \frac{F(r_j^*)}{f(r_j^*)}$ (Krishna 2010)
- E_1^e : $r^* = x_0$ (Jehiel and Lamy 2015)
- E_2 : $r^* \in [\bar{x}, x_0]$
- E_{mix} : $r^* = x_0 - \frac{F(r_j^*)}{f(r_j^*)} - \frac{1-q_1}{q_1 f(r_j^*)}$

Given c , the globally optimal reserve price r^* is continuous and increases in x_0

- **The participants' expected profit:** voluntary setting $\succeq$ mandatory setting if c is sufficiently high to exclude potential bidders
- **The auctioneer's expected profit:** Depending on c and x_0 , either setting can be favored
- **Expected welfare:** $r = x_0$ is welfare maximizing, voluntary setting $\succeq$ mandatory setting

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Conclusion

The current analysis of our model shows advantages of the voluntary setting over the mandatory setting in terms of

- higher expected participation
- higher expected welfare
- higher participants' expected profit if the information cost is sufficiently high
- in certain cases even higher auctioneer's expected profit

Answer to our research question: voluntary setting $\succeq$ mandatory setting

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References I



Bergemann, Dirk and Juuso Välimäki (2002). "Information Acquisition and Efficient Mechanism Design". In: *Econometrica* 70.3, pp. 1007–1033. ISSN: 00129682, 14680262. URL: <http://www.jstor.org/stable/2692306> (visited on 01/26/2025).



Bundestag (2017). *Renewable Energy Sources Act (EEG 2017) - English Version*. accessed March 23rd, 2018. URL: https://www.bmwi.de/Redaktion/EN/Downloads/renewable-energy-sources-act-2017.pdf?__blob=publicationFile&v=3.



Celik, Gorkem and Okan Yilankaya (2009). "Optimal auctions with simultaneous and costly participation". In: *The BE Journal of Theoretical Economics* 9.1, p. 0000102202193517041522.



Compte, Olivier and Philippe Jehiel (2007). "Auctions and information acquisition: sealed bid or dynamic formats?" In: *The Rand Journal of Economics* 38.2, pp. 355–372.



Gillen, Philippe, Vitali Gretschko, and Alexander Rasch (2017). "Pre-auction or post-auction qualification?" In: *Economic Theory Bulletin* 5, pp. 139–150.



Gretschko, Vitali and Jasmina Simon (2024). "An Efficient Dynamic Mechanism with Covert Information Acquisition". In: *ZEW-Centre for European Economic Research Discussion Paper* 24-081.



Gretschko, Vitali and Achim Wambach (2014). "Information acquisition during a descending auction". In: *Economic Theory* 55, pp. 731–751.



Jehiel, Philippe and Laurent Lamy (2015). "On discrimination in auctions with endogenous entry". In: *American Economic Review* 105.8, pp. 2595–2643.

References II



Kreiss, Jan, Karl-Martin Ehrhart, and Marie-Christin Haufe (2017). "Appropriate design of auctions for renewable energy support—Prequalifications and penalties". In: *Energy Policy* 101, pp. 512–520.



Krishna, Vijay (2010). *Auction theory*. 2nd. Academic Press.



Levin, Dan and James L Smith (1994). "Equilibrium in auctions with entry". In: *The American Economic Review*, pp. 585–599.



McAfee, R Preston and John McMillan (1987). "Auctions with entry". In: *Economics Letters* 23.4, pp. 343–347.



Menezes, Flavio M and Paulo K Monteiro (2000). "Auctions with endogenous participation". In: *Review of Economic Design* 5, pp. 71–89.



Persico, Nicola (2000). "Information acquisition in auctions". In: *Econometrica* 68.1, pp. 135–148.



Samuelson, William F. (1985). "Competitive bidding with entry costs". In: *Economics Letters* 17, pp. 53–57. ISSN: 0165-1765. DOI: [http://dx.doi.org/10.1016/0165-1765\(85\)90126-0](http://dx.doi.org/10.1016/0165-1765(85)90126-0).



Schweizer, Nikolaus and Nora Szech (2017). "Revenues and welfare in auctions with information release". In: *Journal of Economic Theory* 170, pp. 86–111.



Stegeman, Mark (1996). "Participation costs and efficient auctions". In: *Journal of Economic Theory* 71.1, pp. 228–259.



Tan, Guofu and Okan Yilankaya (2006). "Equilibria in second price auctions with participation costs". In: *Journal of Economic Theory* 130.1, pp. 205–219.